## Welton Primary School Calculation Progression



The purpose of this document is to provide guidance with teaching pupils to calculate. It contains examples to support the teaching of key mathematical concepts but it not exhaustive and should be used in conjunction with additional models and images to develop a depth of understanding.

#### **Progression in Calculations**

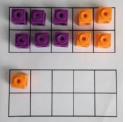
#### **Addition**

Objective and Strategies	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part-part whole model	Use numicon and cubes to add two numbers together as a group or in a har	Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7  10= 6 + 4  Use the part-part whole diagram as shown above to move into the abstract.
Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17  Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17  Place the larger number in your head and count on the smaller number to find your answer.

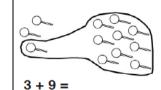
# Regrouping to make 10.



6 + 5 = 11



Start with the bigger number and use the smaller number to make 10.



Use pictures or a number line. Regroup or partition the smaller number to make 10.



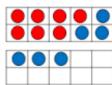
If I am at seven, how many more do I need to make 10. How many more do I add on now?

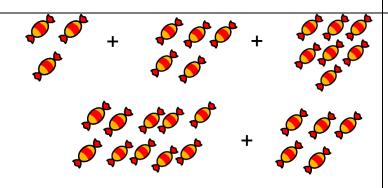


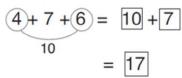


Adding three 4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add single digits on 7.

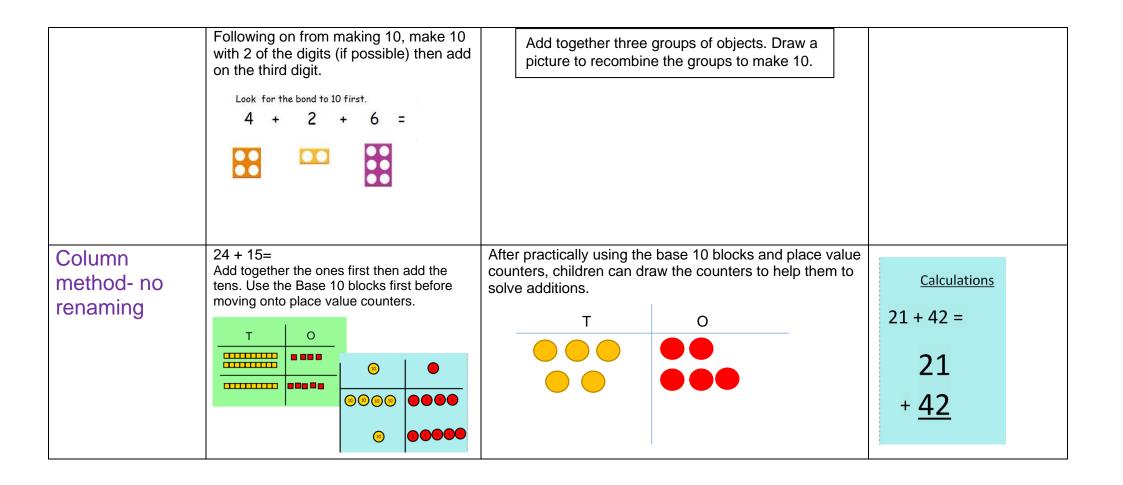






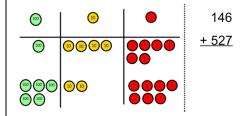


Combine the two numbers that make 10 and then add on the remainder.

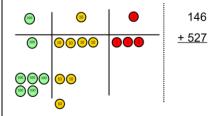


### Column method-renaming

Make both numbers on a place value grid.



Add up the units and exchange 10 ones for one 10.

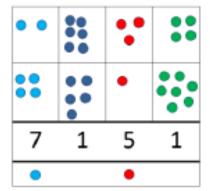


Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.



Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

$$\begin{array}{rrrr} 20 & + & 5 \\ \underline{40} & + & 8 \\ 60 & + & 13 & = 73 \end{array}$$

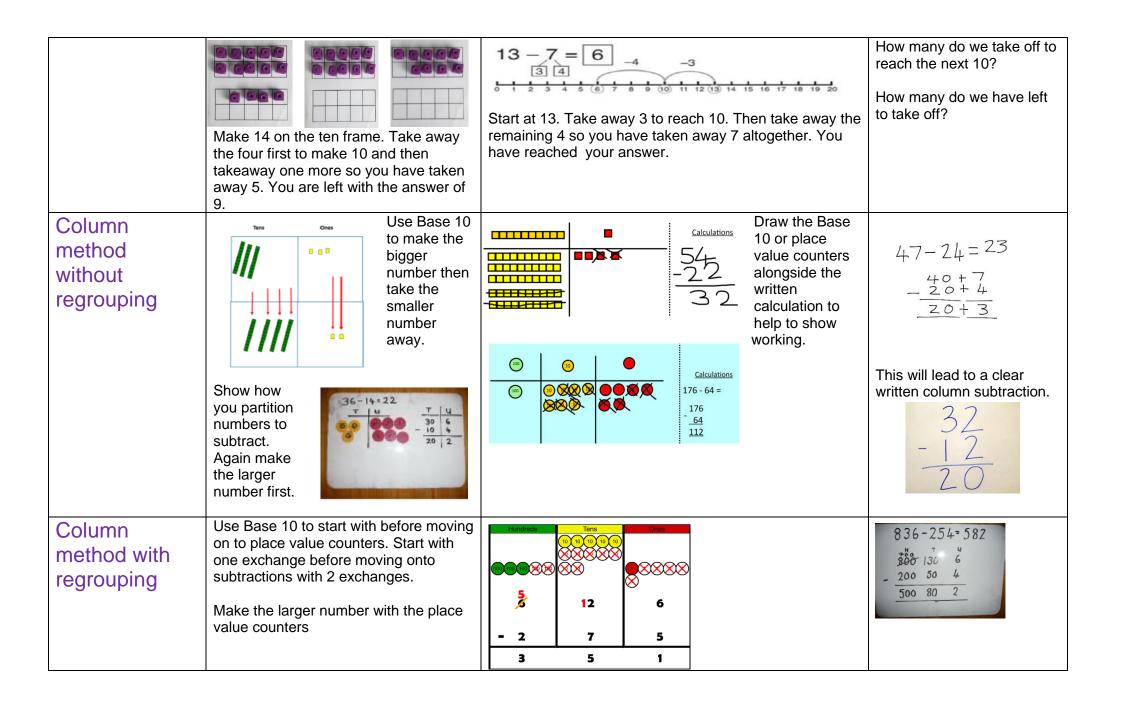
As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.  $\frac{+85}{621}$ 

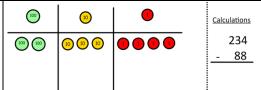
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#### **Subtraction**

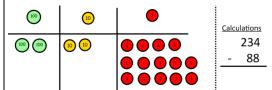
Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. $6-2=4$	Cross out drawn objects to show what has been taken away.	18 -3= 15 8 - 2 = 6
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.	Count back on a number line or number track  9 10 11 12 13 14 15  Start at the bigger number and count back the smaller number showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
	Use counters and move them away from the group as you take them away counting backwards as you go.	This can progress all the way to counting back using two 2 digit numbers.	

Find the	Compare amounts and objects to find		Hannah has 23 sandwiches,
difference	the difference.	+6 Count on to	Ruby has 15 sandwiches.
ullerence		find the difference.	Find the difference between the number of sandwiches.
	Use cubes to	difference.	the number of sandwiches.
	build towers or	0 1 2 3 4 3 6 7 8 9 10 11 12	
	make bars to find the		
	difference	Comparison Bar Models	
	5 Pencils	Draw bars to Lisa is 13 years old. Her sister is 22 years old.	
	Use basic bar models with	tind Find the difference in age between them.	
	items to find	between 2	
	the difference	numbers.	
	3 Erasers ?	Sister	
	<b>1 1 1 1 1 1 1 1 1 1</b>	22	
	4 6 2 3		
	032		
	Link to a difference		
Part-Part	Link to addition- use the part-part whole	Use a pictorial representation of objects to show the part- part whole model.	5
Whole Model	model to help explain	pair imee meesi	
	the inverse between addition and		10
	subtraction.		
	If 10 is the whole and 6 is one of the parts. What is the other part?		Move to using numbers within the part whole model.
	parts. What is the other part:		within the part whole model.
	10 - 6 =		
Make 10	14 – 9 =		16 0_
			16 – 8=

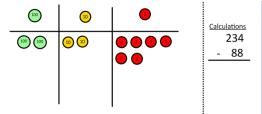




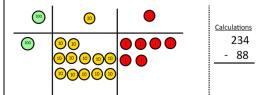
Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



Now I can subtract my ones.



Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction

Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.

When confident, children can find their own way to record the exchange/regrouping.



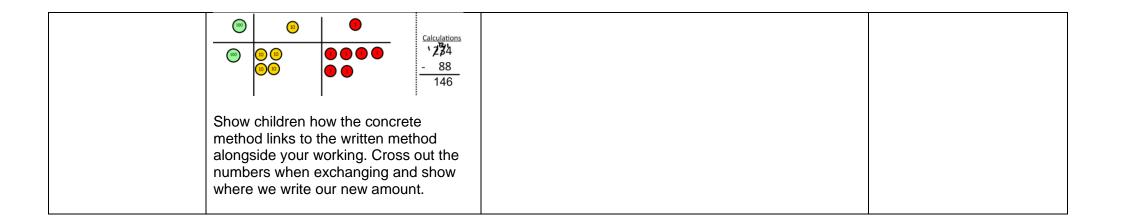
Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup.

Children can start their formal written method by partitioning the number into clear place value columns.



Moving forward the children use a more compact method.

This will lead to an understanding of subtracting any number including decimals.



#### **Multiplication**

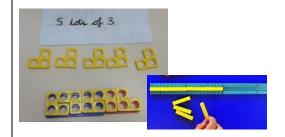
Objective and Strategies	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number.  double 4 is 8  4×2=8	Draw pictures to show how to double a number.  Double 4 is 8	16 10 6 x2 20 12 Partition a number and then double each part before recombining it back together.

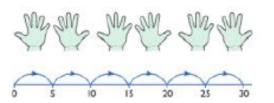
#### Counting in multiples





Count in multiples supported by concrete objects in equal groups.





Use a number line or pictures to continue support in counting in multiples.

Count in multiples of a number aloud.

Write sequences with multiples of numbers.

2, 4, 6, 8, 10

5, 10, 15, 20, 25, 30

#### Repeated addition



Use different objects to add equal groups.

3 + 3 + 3



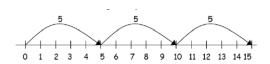
There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?





5 + 5 + 5 = 15

2 add 2 add 2 equals 6



describe objects and pictures.

Write addition sentences to



Arraysshowing commutative multiplication Create arrays using counters/ cubes to show multiplication sentences.





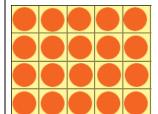
4 rows

4 rows of 3

of 10

4 rows of 13

Draw arrays in different rotations to find **commutative** multiplication sentences.



Link arrays to area of rectangles.

 $2 \times 4 = 8$ 

2 × 4 = 8

00

 $4 \times 2 = 8$ 

Use an array to write multiplication sentences and reinforce repeated addition.



$$5 + 5 + 5 = 15$$

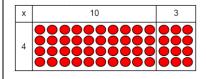
$$3 + 3 + 3 + 3 + 3 = 15$$

$$5 \times 3 = 15$$

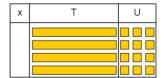
$$3 \times 5 = 15$$

**Grid Method** 

Show the link with arrays to first introduce the grid method.

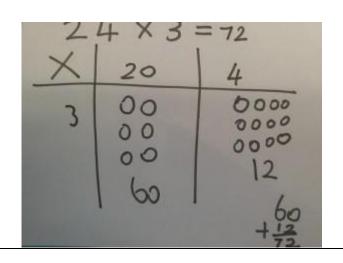


Move on to using Base 10 to move towards a more compact method.



Move on to place value counters to show how we are finding groups of a number.We are multiplying by 4 so we need 4 rows. Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

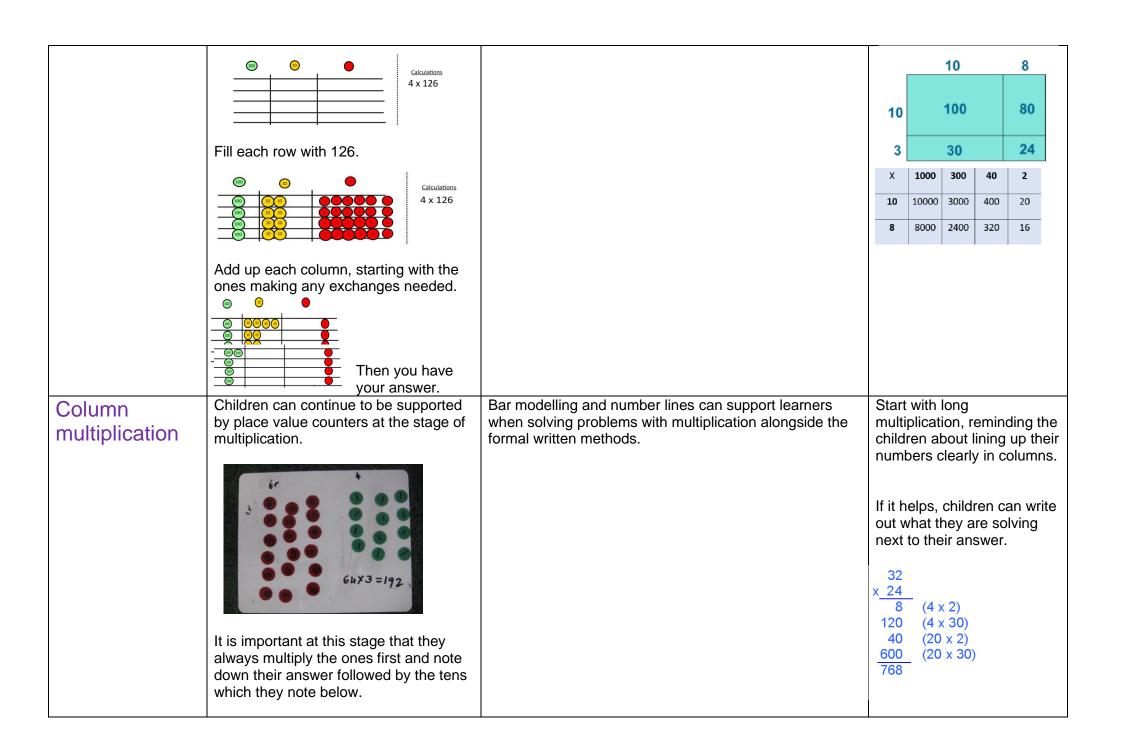


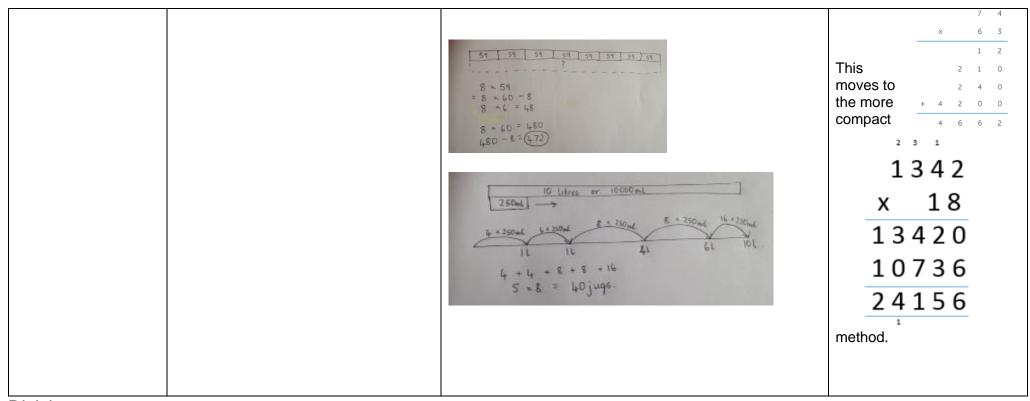
Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.





#### **Division**

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$	Share 9 buns between three people. $9 \div 3 = 3$

#### Division as grouping

Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.





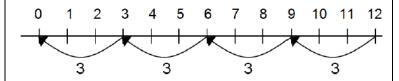
$$96 \div 3 = 32$$



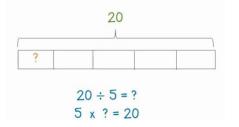




Use a number line to show jumps in groups. The number of jumps equals the number of groups.



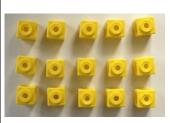
Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.



#### $28 \div 7 = 4$

Divide 28 into 7 groups. How many are in each group?

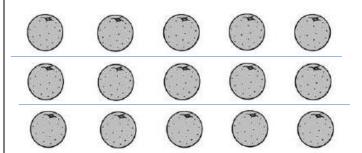
#### Division within arrays



Link division multiplication by creating an array and thinking about the

number sentences that can be created.

Eg 
$$15 \div 3 = 5$$
  $5 \times 3 = 15$   
 $15 \div 5 = 3$   $3 \times 5 = 15$ 



Draw an array and use lines to split the array into groups to make multiplication and division sentences.

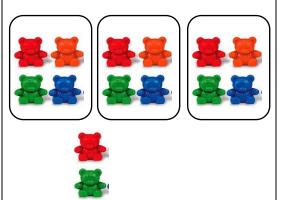
Find the inverse of multiplication and division sentences by creating four linking number sentences.

$$7 \times 4 = 28$$
  
 $4 \times 7 = 28$   
 $28 \div 7 = 4$   
 $28 \div 4 = 7$ 

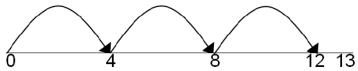
## Division with a remainder Short division

 $14 \div 3 =$ 

Divide objects between groups and see how much is left over



Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



Draw dots and group them to divide an amount and clearly show a remainder.



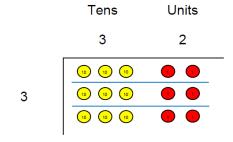




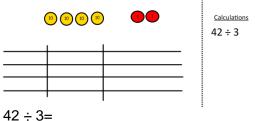


Complete written divisions and show the remainder using r.



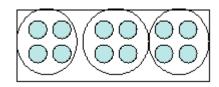


Use place value counters to divide using the bus stop method alongside



Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.

Move onto divisions with a remainder.

